

TECHNICAL APPENDIX BSeasonality

1 As in the R2000-1 models, we modeled seasonality in Priority Mail and Express
2 Mail models using quarterly dummies and two additional seasonal variables for the
3 movement of pre-Christmas days between postal quarters.

4 The Postal Service's fiscal calendar is made up of 13 accounting periods of 28
5 days each. The Postal Service's fiscal calendar is divided into 4 quarters. The first
6 three quarters consist of 3 accounting periods each. The fourth quarter is made up of 4
7 accounting periods. Because of this, the Postal Service's fiscal calendar is made up of
8 364 days and does not change in leap years. Thus, the beginning of the Postal fiscal
9 year as well as the beginning of each postal quarter, shifts over time. The Postal fiscal
10 year begins in the Fall. Postal fiscal year 1970 began on October 18, 1969. Postal
11 fiscal year 1999 began on September 12, 1998.

12 Due to the movement of the Postal quarters within the Gregorian calendar,
13 relative quarterly mail volume changed over time. Mail volumes prior to Christmas are
14 expected to be high. Prior to calendar year 1982, Christmas Day fell in the first Postal
15 quarter. The second Postal quarter of Postal fiscal year 1983 started on Christmas
16 Day of the calendar year 1982. From Postal fiscal year 1983, the number of days prior
17 to Christmas Day in the second Postal quarter has been gradually increasing. The
18 second quarter of Postal fiscal year 1999 began on December 5, 1998 and thus
19 included 15.5 days prior to Christmas Day (Business days exclude Sundays and count

1 Saturdays as half days). Due to the migration of Christmas Day from the first Postal
2 quarter to the second Postal quarter, the Christmas mail volume shares have changed
3 between the first Postal quarter and the second Postal quarter. This migration of
4 Christmas mail from the first Postal quarter to the second Postal quarter is due to the
5 Postal Services moving calendar. So even if the seasonal variation in mail volume is
6 constant, in the Gregorian calendar, it may not be constant in Postal quarters.

7 RCF created a set of seventeen seasonal variables. These seasonal variables
8 are constructed so that for any given quarter, the value of the seasonal variable is set
9 equal to the proportion of business days within the quarter that fall within the quarter of
10 interest. A detailed description of these variables is provided in USPS witness Thomas
11 Thress R97-1 testimony USPS-T-7 pp 125-7.

12 We experimented with these seasonal variables in the Priority Mail and Express
13 Mail models. However, we found that most of the estimated coefficients of these
14 seasonal variables were of unexpected sign. In our model we used the quarterly fixed
15 seasonal dummies for Fall, Winter, Spring, and two additional seasonal variables to
16 capture the moving Christmas Day effect. The two additional seasonal variables were
17 constructed in the same way as RCF's seasonal variables. The first seasonal variable
18 covered the period from December 1 through December 23, while the second seasonal
19 variable covered the period from December 24 through January 1. In the recent history
20 Priority Mail volume has been increasing in the second postal quarter compared to the
21 first postal quarter. To allow for this additional Christmas Day effect the seasonal
22 variable covering the period from December 1 through December 23 was added to the

1 Priority Mail model beginning in 1997. The estimated coefficients of these seasonal
 2 variables had the expected sign. The first seasonal variable covering the period prior
 3 to Christmas Day was positive as expected, and statistically significant in both Priority
 4 Mail and Express Mail models. The second seasonal variable covering the period from
 5 a day before Christmas Day to the first day of January was negative as expected and
 6 statistically significant in Priority Mail but not statistically significant in the Express Mail
 7 model. The third seasonal variable used only in the Priority Mail model covering the
 8 period prior to Christmas Day beginning in 1997 was positive and statistically
 9 significant.

10 The estimated effects of the three seasonal dummies and the additional
 11 seasonal variables are combined into a single seasonal index by Postal quarters. The
 12 method of computing this index is described in detail below:

13
 14 Step 1: Multiply the estimated coefficients by the value of the variables and sum
 15 across each quarter. For example, the estimated coefficient and the
 16 values of the variables in the Priority Mail model are:

	FALL	WINTER	SPRING	DEC1_23	DEC24_JAN1	DDEC1_23
Coefficients	0.0658420	0.0763942	0.0887914	0.2766378	-0.6667887	0.3448305
Values						
1988:1	1.000000	0.000000	0.000000	0.234375	0.000000	0.000000
1988:2	0.000000	1.000000	0.000000	0.054688	0.085938	0.000000
1988:3	0.000000	0.000000	1.000000	0.000000	0.000000	0.000000
1988:4	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000

	FALL	WINTER	SPRING	DEC1_23	DEC24_JAN1	DDEC1_23
Coefficients	0.0658420	0.0763942	0.0887914	0.2766378	-0.6667887	0.3448305
Values						
1999:1	1.000000	0.000000	0.000000	0.062500	0.000000	0.062500
1999:2	0.000000	1.000000	0.000000	0.226563	0.085938	0.226563
1999:3	0.000000	0.000000	1.000000	0.000000	0.000000	0.000000
1999:4	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
2000:1	1.000000	0.000000	0.000000	0.046875	0.000000	0.046875
2000:2	0.000000	1.000000	0.000000	0.242188	0.078125	0.242188
2000:3	0.000000	0.000000	1.000000	0.000000	0.000000	0.000000
2000:4	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000

The sum of the product of the coefficients and variables gives

1988:1 0.130679 This equals $0.066*1 + 0.076*0 + 0.089*0 + 0.277*0.234 - 0.667*0.000 + 0.345*0.000$
 1988:2 0.034221 This equals $0.066*0 + 0.076*1 + 0.089*0 + 0.277*0.055 - 0.667*0.086 + 0.345*0.000$
 1988:3 0.088791 This equals $0.066*0 + 0.076*0 + 0.089*1 + 0.277*0.000 - 0.667*0.000 + 0.345*0.000$
 1988:4 0.000000 This equals $0.066*0 + 0.076*0 + 0.089*0 + 0.277*0.000 - 0.667*0.000 + 0.345*0.000$

1999:1 0.104684 This equals $0.066*1 + 0.076*0 + 0.089*0 + 0.277*0.063 - 0.667*0.000 + 0.345*0.063$
 1999:2 0.159893 This equals $0.066*0 + 0.076*1 + 0.089*0 + 0.277*0.227 - 0.667*0.086 + 0.345*0.227$
 1999:3 0.088791 This equals $0.066*0 + 0.076*0 + 0.089*1 + 0.277*0.000 - 0.667*0.000 + 0.345*0.000$
 1999:4 0.000000 This equals $0.066*0 + 0.076*0 + 0.089*0 + 0.277*0.000 - 0.667*0.000 + 0.345*0.000$
 2000:1 0.094973 This equals $0.066*1 + 0.076*0 + 0.089*0 + 0.277*0.047 - 0.667*0.000 + 0.345*0.047$
 2000:2 0.174813 This equals $0.066*0 + 0.076*1 + 0.089*0 + 0.277*0.242 - 0.667*0.078 + 0.345*0.242$
 2000:3 0.088791 This equals $0.066*0 + 0.076*0 + 0.089*1 + 0.277*0.000 - 0.667*0.000 + 0.345*0.000$
 2000:4 0.000000 This equals $0.066*0 + 0.076*0 + 0.089*0 + 0.277*0.000 - 0.667*0.000 + 0.345*0.000$

Step 2: Take the anti-log of the above series

1988:1 1.139602 This equals EXP(0.130679)
 1988:2 1.034813 This equals EXP(0.034221)
 1988:3 1.092853 This equals EXP(0.088791)
 1988:4 1.000000 This equals EXP(0.000000)

1999:1 1.110359 This equals EXP(0.104684)
 1999:2 1.173386 This equals EXP(0.159893)
 1999:3 1.092853 This equals EXP(0.088791)

1	1999:4	1.000000	This equals	EXP(0.000000)
2	2000:1	1.099630	This equals	EXP(0.094973)
3	2000:2	1.191024	This equals	EXP(0.174813)
4	2000:3	1.092853	This equals	EXP(0.088791)
5	2000:4	1.000000	This equals	EXP(0.000000)

6

7 Step 3: Compute the weighted values of the index using number of business days
8 as the weights.

9			Business			
10			Days in	Business		
11			quarter	Days in PFY		
12	1988:1	0.261414	64	279	This equals	1.139602*64/279
13	1988:2	0.237376	64	279	This equals	1.034813*64/279
14	1988:3	0.254607	65	279	This equals	1.092853*65/279
15	1988:4	0.308244	86	279	This equals	1.000000*86/279
16	1999:1	0.254706	64	279	This equals	1.110359*64/279
17	1999:2	0.269164	64	279	This equals	1.173386*64/279
18	1999:3	0.258524	66	279	This equals	1.092853*66/279
19	1999:4	0.304659	85	279	This equals	1.000000*85/279
20	2000:1	0.252245	64	279	This equals	1.099630*64/279
21	2000:2	0.273210	64	279	This equals	1.191024*64/279
22	2000:3	0.258524	66	279	This equals	1.092853*66/279
23	2000:4	0.304659	85	279	This equals	1.000000*85/279

24

25 Step 4: Compute the weighted annual sum.

26	1988:1	1.061641	This equals	0.26141+0.23738+0.25461+0.30824
27	1988:2	1.061641	This equals	0.26141+0.23738+0.25461+0.30824
28	1988:3	1.061641	This equals	0.26141+0.23738+0.25461+0.30824
29	1988:4	1.061641	This equals	0.26141+0.23738+0.25461+0.30824
30	1999:1	1.087054	This equals	0.25471+0.26916+0.25852+0.30466
31	1999:2	1.087054	This equals	0.25471+0.26916+0.25852+0.30466
32	1999:3	1.087054	This equals	0.25471+0.26916+0.25852+0.30466
33	1999:4	1.087054	This equals	0.25471+0.26916+0.25852+0.30466
34	2000:1	1.088638	This equals	0.25224+0.27321+0.25852+0.30466

1 2000:2 1.088638 This equals 0.25224+0.27321+0.25852+0.30466
 2 2000:3 1.088638 This equals 0.25224+0.27321+0.25852+0.30466
 3 2000:4 1.088638 This equals 0.25224+0.27321+0.25852+0.30466

4

5 Step 5: Divide the values of the seasonal index from step 2 by the weighted
 6 annual sum from step 4.

7 1988:1 1.073434 This equals 1.13960/1.06164
 8 1988:2 0.974729 This equals 1.03481/1.06164
 9 1988:3 1.029399 This equals 1.09285/1.06164
 10 1988:4 0.941938 This equals 1.00000/1.06164

11 1999:1 1.021439 This equals 1.11036/1.08705
 12 1999:2 1.079419 This equals 1.17339/1.08705
 13 1999:3 1.005335 This equals 1.09285/1.08705
 14 1999:4 0.919918 This equals 1.00000/1.08705
 15 2000:1 1.010096 This equals 1.09963/1.08864
 16 2000:2 1.094049 This equals 1.19102/1.08864
 17 2000:3 1.003871 This equals 1.09285/1.08864
 18 2000:4 0.918579 This equals 1.00000/1.08864

19

20 Step 6: Since the forecasts are quarterly we need to adjust the index to reflect
 21 that quarters one, two and three have three accounting periods each,
 22 while quarter four has four accounting periods. So we compute the
 23 weighted values of the index using the number of accounting periods per
 24 quarter as the weights.

			Number of		
			APs in	Number of	
			quarter	APs in PFY	
25					
26					
27					
28	1988:1	0.247716	3	13	This equals 1.073434*3/13

1	1988:2	0.224938	3	13	This equals $0.974729 \times 3/13$
2	1988:3	0.237554	3	13	This equals $1.029399 \times 3/13$
3	1988:4	0.289827	4	13	This equals $0.941938 \times 4/13$
4	1999:1	0.235717	3	13	This equals $1.021439 \times 3/13$
5	1999:2	0.249097	3	13	This equals $1.079419 \times 3/13$
6	1999:3	0.232000	3	13	This equals $1.005335 \times 3/13$
7	1999:4	0.283052	4	13	This equals $0.919918 \times 4/13$
8	2000:1	0.233099	3	13	This equals $1.010096 \times 3/13$
9	2000:2	0.252473	3	13	This equals $1.094049 \times 3/13$
10	2000:3	0.231663	3	13	This equals $1.003871 \times 3/13$
11	2000:4	0.282640	4	13	This equals $0.918579 \times 4/13$
12					

13 Step 7: Compute the weighted annual sum.

14					
15	1988:1	1.000034	This equals	$0.24772+0.22494+0.23755+0.28983$	
16	1988:2	1.000034	This equals	$0.24772+0.22494+0.23755+0.28983$	
17	1988:3	1.000034	This equals	$0.24772+0.22494+0.23755+0.28983$	
18	1988:4	1.000034	This equals	$0.24772+0.22494+0.23755+0.28983$	
19	1999:1	0.999865	This equals	$0.23572+0.24910+0.23200+0.28305$	
20	1999:2	0.999865	This equals	$0.23572+0.24910+0.23200+0.28305$	
21	1999:3	0.999865	This equals	$0.23572+0.24910+0.23200+0.28305$	
22	1999:4	0.999865	This equals	$0.23572+0.24910+0.23200+0.28305$	
23	2000:1	0.999874	This equals	$0.23310+0.25247+0.23166+0.28264$	
24	2000:2	0.999874	This equals	$0.23310+0.25247+0.23166+0.28264$	
25	2000:3	0.999874	This equals	$0.23310+0.25247+0.23166+0.28264$	
26	2000:4	0.999874	This equals	$0.23310+0.25247+0.23166+0.28264$	

27

28 Step 8: Divide the values of the seasonal index from step 5 by the weighted

29 annual sum from step 7 to obtain the final values of the seasonal index.

30	1988:1	1.073398	This equals	$1.07343/1.000034$
31	1988:2	0.974696	This equals	$0.97473/1.000034$

1	1988:3	1.029364	This equals	1.02940/1.000034
2	1988:4	0.941906	This equals	0.94194/1.000034
3	1999:1	1.021577	This equals	1.02144/0.999865
4	1999:2	1.079564	This equals	1.07942/0.999865
5	1999:3	1.005470	This equals	1.00533/0.999865
6	1999:4	0.920042	This equals	0.91992/0.999865
7	2000:1	1.010223	This equals	1.01010/0.999874
8	2000:2	1.094187	This equals	1.09405/0.999874
9	2000:3	1.003998	This equals	1.00387/0.999874
10	2000:4	0.918694	This equals	0.91858/0.999874

11

12 This index shows the quarterly seasonal pattern and the change in seasonal
13 pattern overtime. The values of the seasonal index in 1988 are:

14	1988:1	1.073398
15	1988:2	0.974696
16	1988:3	1.029364
17	1988:4	0.941906

18

19 So in 1988 the volume in the first postal quarter is the highest. It is no surprise
20 as the first eighteen days of December are included in the first Postal quarter of 1988.
21 As we move through the years the value of the index in 1998 is the highest in the
22 second Postal quarter. Again this is no surprise as the second quarter of 1998
23 includes Postal volume from December 5, onwards. Thus the index clearly shows the
24 transfer of Postal volume from the first Postal quarter to the second Postal quarter over
25 time. The advantage of using a seasonal index for forecasting Postal volumes is that
26 the index reallocates the forecasts based on the seasonal pattern within each year and
27 does not changes the volume from year to year. This can be seen by weighing each

1 index value by the proportion of accounting periods in the Postal quarter and summing
 2 the result. For example,

3	1988:1	0.247707	This equals	$1.07340 \times 3/13$
4	1988:2	0.224930	This equals	$0.97470 \times 3/13$
5	1988:3	0.237546	This equals	$1.02936 \times 3/13$
6	1988:4	0.289817	This equals	$0.94191 \times 4/13$
7		1.000000	This equals	$0.24771 + 0.22493 + 0.23755 + 0.28982$
8				
9	1999:1	0.235749	This equals	$1.02158 \times 3/13$
10	1999:2	0.249130	This equals	$1.07956 \times 3/13$
11	1999:3	0.232032	This equals	$1.00547 \times 3/13$
12	1999:4	0.283090	This equals	$0.92004 \times 4/13$
13		1.000000	This equals	$0.23575 + 0.24913 + 0.23203 + 0.28309$
14				
15	2000:1	0.233128	This equals	$1.01022 \times 3/13$
16	2000:2	0.252505	This equals	$1.09419 \times 3/13$
17	2000:3	0.231692	This equals	$1.00400 \times 3/13$
18	2000:4	0.282675	This equals	$0.91869 \times 4/13$
19		1.000000	This equals	$0.23313 + 0.25250 + 0.23169 + 0.28268$

20